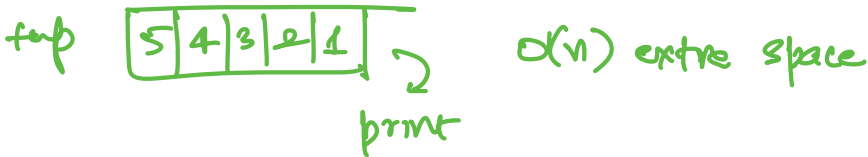


Space Complexity:

Input array } Not used in extra space



Generally, Time & Space Tradeoff

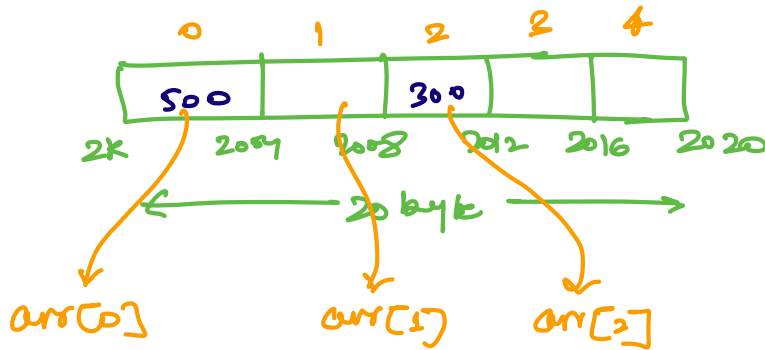
ARRAYS:

1D:

```
int arr[5];
```

↳ homogeneous collection

1 int \rightarrow 4 byte
5 int \rightarrow 20 byte



$arr[2] = 300$

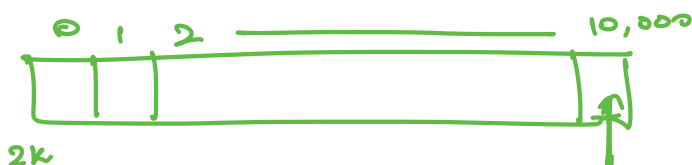
base address + (idx * int size)

$2000 + (2 * 4) = 2008$

constant time

$arr[0] = 500$

$2000 + (0 * 4) = 2000$

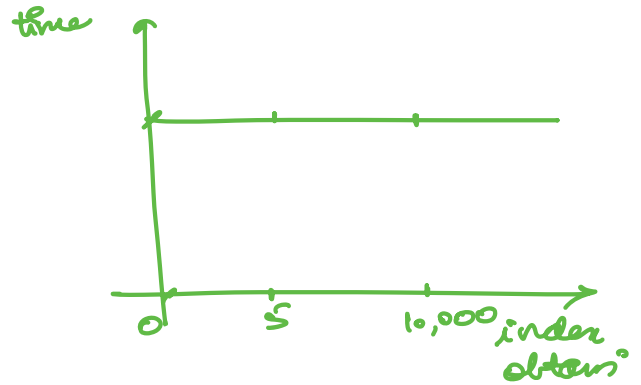


10,001 size

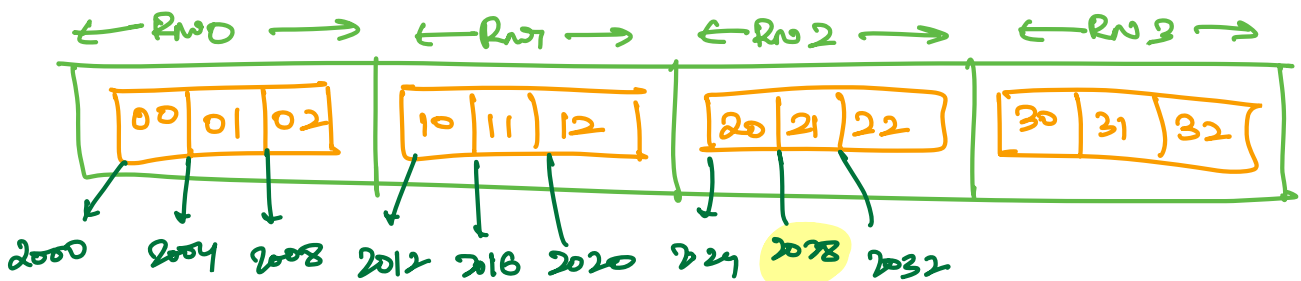
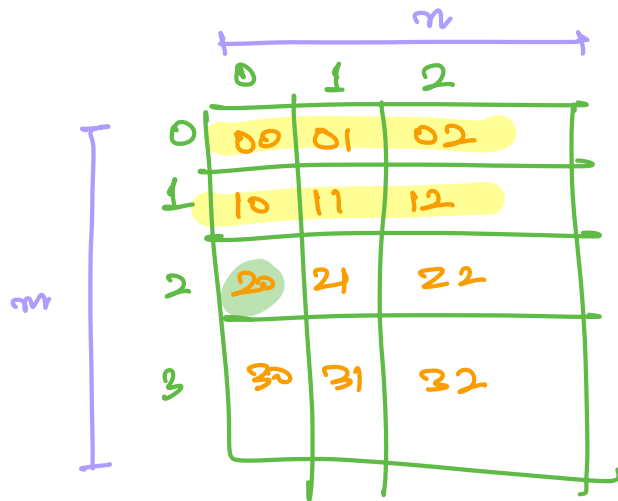
$2k + (10000 * 4) = \underline{\hspace{2cm}}$

Array index update, obtain : $O(1)$
get/set

To reach 10,000 index you don't do linear traversal X
 instead calculation, jump to memory location.



2D Arrays
 ↙
 Row Major Order
 ↘
 Column Major Order



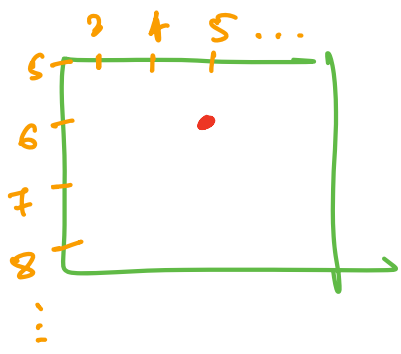
`cout << arr[2][1]`
 i j

$$2000 + ((2 * 3) + 1) * \text{int size}$$

$$2000 + (7 * 4) = 2028$$

m rows
n columns
m x n

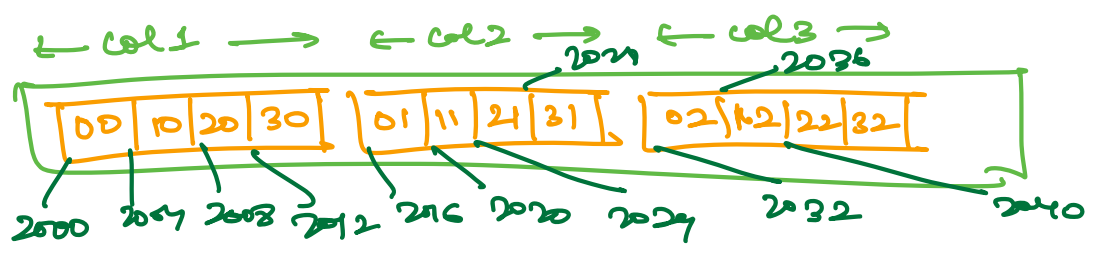
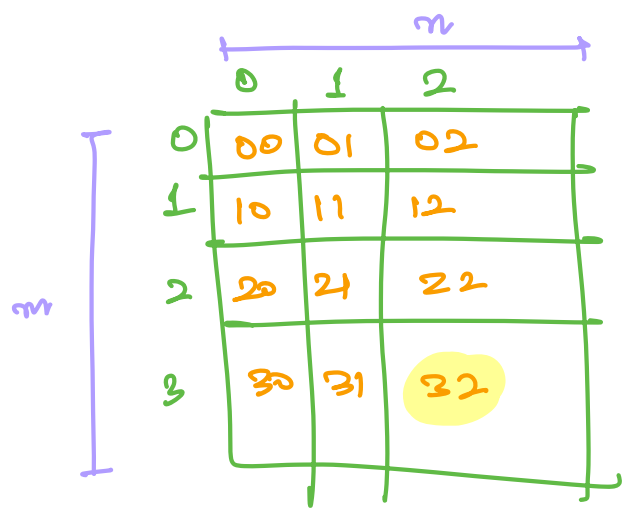
$$(i, j \text{ cell}) \rightarrow \boxed{\text{base address} + (i * n + j) * \text{data type size}}$$



lr=5 lc=3 (i,j) cell

$$\boxed{\text{base address} + ((i - lr) * n + (j - lc)) * \text{size}}$$

Column major order



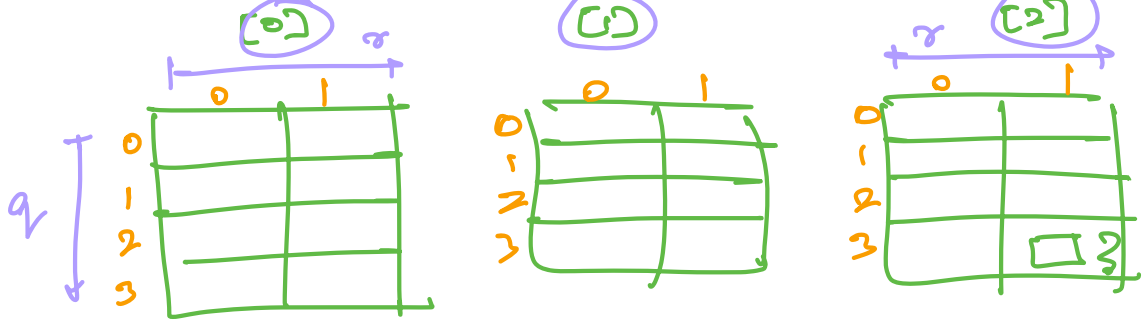
3,2 :
(i,j)

$$\boxed{\text{base address} + (j * m + i) * \text{size}}$$

3D Arrays

```
int arr[3][4][2]
```

: 3, 2D Arrays of size 4x2



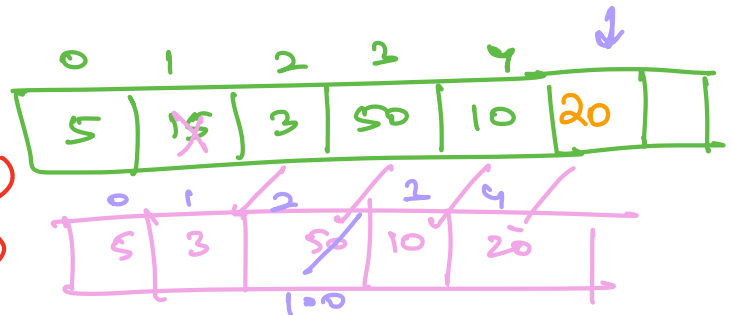
$arr[i][j][k]$?

$$\text{base address} + (i * q * r + j * r + k) * \text{int size}$$

Array operations

Unsorted

- Insert $\rightarrow arr[i]: \text{item} : O(1)$
- Delete $\rightarrow \text{item is ?} : O(n)$
- Update $\rightarrow \text{2 index} \rightarrow 100$
 $arr[2] = 100 \quad O(1)$

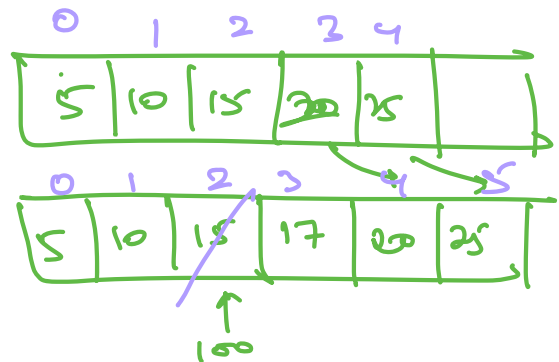


- Min $\rightarrow \text{loop} \quad O(n)$
- Max $\rightarrow \text{loop} \quad O(n)$
- \rightarrow Find $\rightarrow \text{loop} \quad O(n)$

Sorted

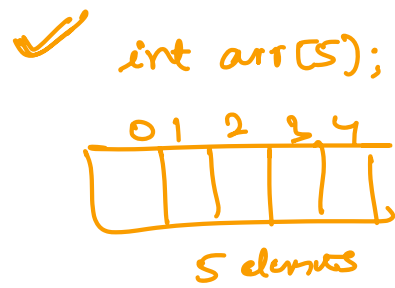
- Insert $\rightarrow \text{17 insert} \quad O(n)$
- Delete $O(n)$
- Update $arr[2] = 100 \quad O(1)$

- Min $: O(1)$ 0 index
- Max $: O(1)$ last index
- \rightarrow Find $: O(\log n)$



Dynamic Arrays

C++: vectors
Java: ArrayList



DA: size don't have to worry.

vector `<int> v;` $\xrightarrow{\text{internally array}}$

| | Size | Capacity | |
|---------------------------|------|----------|------------|
| | 0 | 2 | |
| <code>pushback(10)</code> | 1 | 2 | |
| <u><code>(20)</code></u> | 2 | 2 | |
| <u><code>(30)</code></u> | 3 | 4 | 2 copy + 1 |
| <u><code>(40)</code></u> | 4 | 4 | 1 |
| <u><code>(50)</code></u> | 5 | 8 | 4 copy + 1 |
| 4 push-back | 6 | 8 | 1 |
| | 7 | 8 | 1 |
| | 8 | 8 | 1 |
| | 9 | 16 | |

You can decide?

2 push-back = 4 ops
4 push-back = 8 ops

1 push-back \rightarrow 2 ops
1 push-back \rightarrow 2 ops } $O(1)$

Inert: Size == Capacity Double size array copy.

Delete: Size = Cap/2 Array half

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 |

S=8 C=8

delete 10 20 30 40 50 60 70 -

S=7 C=8

delete 10 20 30 40 50 60 - -

S=6 C=8

delete 10 20 30 40 50 - - -

S=5 C=8

delete 10 20 30 40 - - -

S=4 C=8

(4)

| | | | |
|----|----|----|----|
| 10 | 20 | 30 | 40 |
|----|----|----|----|

S=4 C=4

add 4+1 10 20 30 40 50 - - -

C=5 C=8

delete 4 10 20 30 40

S=4 C=4

add 4+1 10 20 30 40 50 - - -

S=5 C=8

→ $4+4+4+4+2^x$

4 push-pop → $\frac{4 \cdot 4}{16 \cdot 2}$

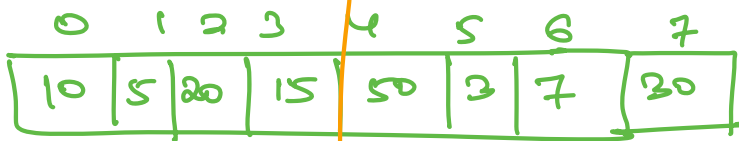
4 → $\frac{4 \cdot 4}{16} = m$

Size = Cap/4 Array half

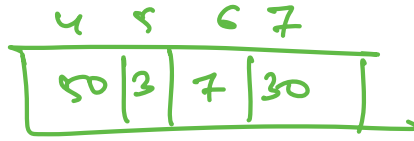
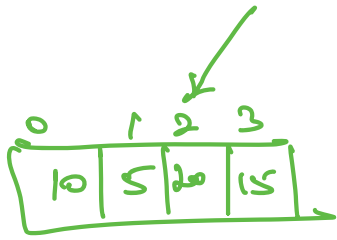
Linear Search | B.S, S.S, IS
Binary Search

Merge sort

Divide & Conquer Algo



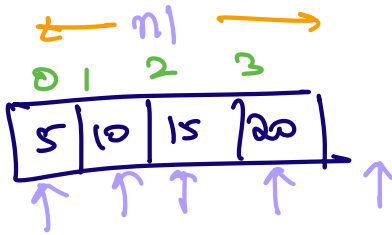
Divide



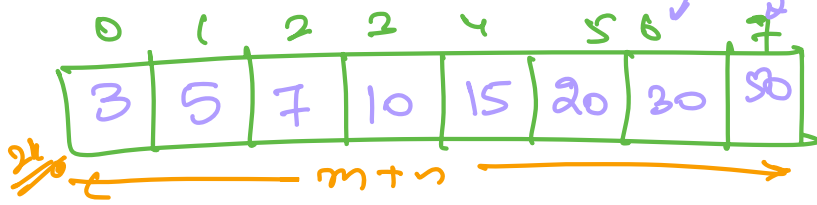
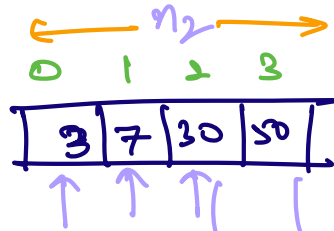
merge 2 sorted arrays

Q:

arr1

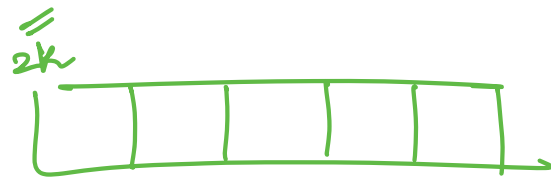
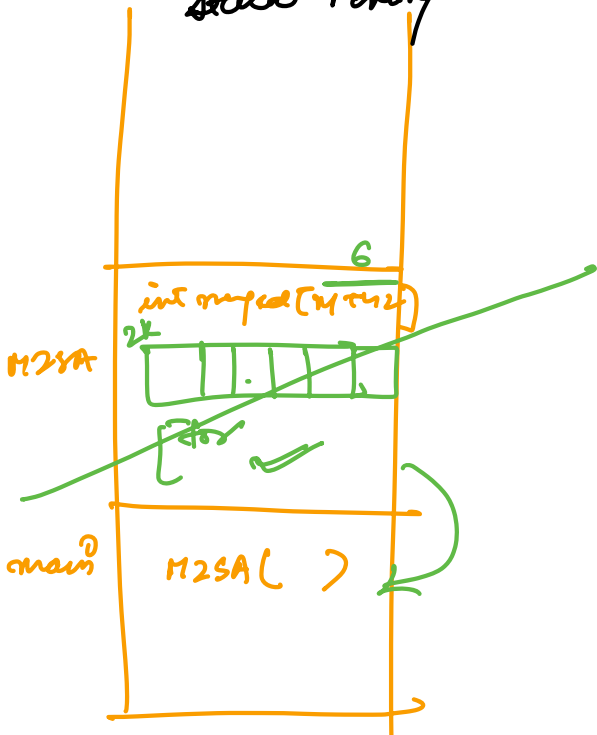


arr2



Stack Memory

Heap Memory



new → Heap
int *merged = new int(5);
2k
"

vector<int> v;

vector<int> v = new vector ();